EXPERIMENTAL STUDY OF THERMAL CONDUCTIVITY OF NEON-HELIUM MIXTURES

AT HIGH TEMPERATURES

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Experimental data on the thermal conductivity of neon-helium mixtures in the temperature range 350-1500°K are presented. Above 800°K these are the first such experimentally obtained data.

The study of the thermal conductivity of monatomic gases and their mixtures over a wide temperature range is of significant interest for the development and refinement of theory, while also having major practical importance.

Knowledge of the thermophysical characteristics of monatomic gases and their mixtures is necessary in gas-laser construction in order to calculate heat flow from cathode to anode, from the sections forming the capillary channel and to design heaters, etc.

The temperature dependence of the thermal conductivity of neon-helium mixtures has been studied inadequately [4], and at temperatures below 0°C no data are available. The range 273-363°K has been studied most thoroughly, but even there the majority of authors measured the thermal conductivity of the He-Ne mixture at one of two definite temperatures [5-9, 12], i.e., the concentration dependence of thermal conductivity of the given mixture was studied. In [10] the hot-wire method was used for the first time to study the temperature dependence of thermal conductivity of an He-Ne mixture at three concentrations (0.2566, 0.4560, and 0.7552Ne) in the temperature range 303-363°K to an accuracy of $\pm 2\%$. Saxena and Tondon [11] presented smoothed and interpolated thermal-conductivity values from [10] for neon-helium mixtures (0.2, 0.4, 0.6, and 0.8Ne).

In [9], the thermal conductivity of an He-Ne mixture was measured by the hot-wire method at two temperatures - 302 and 793°K - to an accuracy of $\pm 2\%$. This was the first experimental measurement at a significantly high temperature. The experimental thermal-conductivity values of the He-Ne mixture at 302°K in [9] are systematically higher than the experimental data of [10, 11] (Fig. 1) (mean deviation comprises 3.6%).

The thermal conductivity of an He-Ne mixture was first measured by the hot-wire method in 1953 at a temperature of 273°K [5, 6]. The authors of [5, 6] obtained an empirical equation for calculation of the concentration dependence of thermal conductivity. The values calculated with this equation differ from experiment by $\pm 1.2\%$. In [7, 8] the thermal conductivity of this mixture at 291°K was studied with a katharometer calibrated with the thenavailable data on the thermal conductivity of argon-helium mixtures [13]. The measurement uncertainty was not presented, but comparison shows that the data of [7, 8] are significantly higher in value than the results of others. The present authors used graphical correlation to smooth and interpolate the values of [7, 8], demonstrating that for the four mixtures (0.2, 0.4, 0.6, and 0.8Ne) the value lie an average of 9% above those of [10, 11], upon which the correlation at these temperatures was based [2]. In [12], the thermal conductivity of an He-Ne mixture was first studied at a temperature of 297.1°K by the nonstationary cylindrical-probe method with a linear heat source (the technique, theory, and apparatus are described in detail in [14]). As for the experimental data of [12], they are systematically low in comparison with other data. The mean deviation for the four mixtures comprises not less than 14% [2].

On the basis of the above, it may be concluded that at the present time the thermal conductivity of neon-helium mixtures has not been studied sufficiently even in the room-temperature range. The thermal-conductivity of the pure gases helium and neon has been studied by the authors previously [1, 3]. In determining the thermal conductivity of the neon-helium

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Fig. 1. Temperature dependence of thermal conductivity of neon-helium mixtures: 1) data of [9]; 2) [10]; 3) [12]; 4) experiment; 5, 6) results of present study [5) smoothed values; 6) calculation (exp-6)]; $\lambda \cdot 10^3$, W/m·°K; \overline{T} , °K.

Fig. 2. Concentration dependence of thermal conductivity of neon-helium mixtures at "rounded" temperature values: 1) 400°K; 2) 500; 3) 600; 4) 700; 5) 800; 6) 900; 7) 1000; 8) 1100; 9) 1200; 10) 1300; 11) 1400; 12) 1500°K.

mixtures, all factors which distort the true value of the measured quantity were considered, as described in [2]. Therefore, we will dwell only on the corrections which have the most significant effects at high temperatures. For the heaviest of the mixtures studied (0.8Ne-0.2He), the radiation correction increased with temperature from tenths of a percent at 365°K to 8.5% at 1265°K. The correction for temperature shift was determined experimentally over the entire temperature range of 350-1500°K and the pressure range 100 mbar to 1 bar. The largest correction for temperature shift was observed in the case of the lightest mixture (0.2Ne-0.8He), comprising ~24% at T = 1502°K. It should be noted that for all the neonhelium mixtures studied the absolute value of the temperature-shift correction is greater than that for radiation (Table 1). This is explained by the fact that neon-helium mixtures are the lightest of all mixtures of monatomic gases.

Figure 1 shows the thermal-conductivity data obtained in the present study for the temperature range 350-1500°K at a pressure of 1 bar. The mixtures were prepared from highpurity helium (99.993%) with the following impurity content (in percent): neon, 0.002; hydrogen, 0.002; nitrogen, 0.002; oxygen, 0.0005; and hydrocarbons, 0.0005. The neon used was of 99.882% purity with hydrogen content 0.001%; helium, 0.1%; oxygen, 0.001%; nitrogen, 0.01%; and moisture not more than 0.02 g/cm³.

The thermal conductivity of the mixtures (0.2, 0.4, 0.6, and 0.8Ne) were measured over different temperature ranges: 336-1502, 349-1493, 359-1326, and 365-1265°K. The 0.2Ne-0.8He mixture was thus studied over the widest range, while the range of study of the 0.8Ne-0.2He was the narrowest (with a maximum temperature of 1265°K).

The experimental data obtained can be compared with the single available experimental thermal-conductivity value of [9], obtained at 793°K. The data of [9] are systematically higher as compared to ours (Fig. 1). The deviations for the four mixtures (0.2, 0.4, 0.6, and 0.8Ne) comprise 7.3%, 7.6%, 6.8%, and 4.6%, respectively. The experimental data obtained in the present study "join" quite well with the values of [10, 11] in the moderate temperature range (363°K).

TABLE 1. Measurement Data and Experimental Values of Coefficient of Thermal Conductivity for Neon-Helium Mixtures at p = 1 bar

™ _{wa} , °K	Т _{W.} i, •К	т _g , °К	<i>₸</i> , %	Q-10*, W	Q _r ∙10*, W	Q _C .10*, W	λ·10³, W/m•°K	87 _{sh} , %		
0,2Ne 0,8He										
331,7 382,5 475,4 592,3 719,5 893,8 1003,8 1094,9 1177,5 1298,5 1404,0 1499,2	340,99 391,7 484,49 601,28 728,38 902,54 1012,48 1103,55 1186,13 1307,10 1412,59 1507,76	9,22 9,08 8,87 8,61 8,36 7,87 7,57 7,40 7,40 7,40 7,40 6,92 6,69 6,51	336 387 480 597 724 898 1008 1098 1181 1302 1407 1502	107823 118866 134352 153898 169441 191791 199472 207144 213977 225585 231768 240551	54 95 222 536 1147 2694 4237 6007 8057 11812 16126 21038	107775 118771 134130 153362 168294 189097 195235 201137 205920 213773 215642 219513	126 141 163 192 217 259 278 293 310 333 347 363	0,8 1,3 2,4 4,1 5,8 9,9 12,8 14,5 17,0 19,5 22,1 24,0		
			0,	4Ne — 0,6I	He					
344,1 406,7 505,8 594,0 706,1 804,2 910,6 1057,0 1191,3 1268,4 1396,9 1488,5	354,6 417,16 516,19 604,35 716,42 814,5 920,87 1067,22 1201,49 1278,57 1407,03 1498,61	$10,41 \\ 10,31 \\ 10,13 \\ 9,97 \\ 9,78 \\ 9,60 \\ 9,33 \\ 8,97 \\ 8,66 \\ 8,50 \\ 8,24 \\ 8,07$	349 412 511 599 711 809 915 1061 1196 1196 1197 1401 1493	99538 109117 126750 139476 159115 168656 183490 194257 210788 217019 225927 242809	70 140 331 625 1248 2114 3455 6201 9949 12779 18762 24207	99468 108977 126419 138851 157867 166542 180035 188056 200839 204240 207165 218602	103 114 135 150 174 187 208 226 250 259 271 232	0.9 1,4 2,5 3,7 5,2 6,8 9,2 12,2 15,0 16,5 18,7 20,2		
			0,	6Ne — 0,41	le					
353,4 447,9 583,3 679,0 797,1 917,7 1034,9 1155,0 1321,6	364,63 459,09 594,44 690,11 808,17 928,72 1045,88 1165,94 1332,47	11,13 11,01 10,77 10,63 10,41 10,13 9,85 9,60 9,22	359 453 589 684 802 923 1040 1160 1326	87952 100526 122523 132305 148017 162619 169128 185515 194965	86 222 630 1152 2190 3799 6104 9453 16198	87866 100304 121893 131153 145827 158820 163024 176062 178767	85,1 98,2 122 133 151 169 178 198 209	0,9 1,6 3,3 4,3 6,0 8,1 10,3 12,2 15,2		
0,8Ne 0,2He										
358,6 471,5 618,6 730,1 865,7 988,5 1117,4 1259,5	370,7 483,55 630,60 742,07 877,64 1000,40 1129,25 1271,30	12,00 11,85 11,59 11,41 11,19 10,92 10,69 10,33	365 477 624 736 871 994 1123 1265	77137 91423 108377 121276 139283 146388 165683 172082	100 290 858 1665 3298 5575 8997 14546	77037 91133 107519 119611 135985 140813 156686 157546	69,2 82,9 100 113 131 139 158 164	0,9 1,7 3,4 4,7 6,3 8,2 9,8 12,5		

The experimental values obtained in the present study were compared with theoretical values calculated using the formulas of strict molecular-kinetic theory [15] with various potential functions [Lennard-Jones, Buckingham (exp-6), and Morse] and corresponding potential parameters (Table 2). The divergence among calculated values obtained with the various potential functions is insignificant. The theoretical thermal-conductivity values obtained with the Lennard-Jones (12-6) potential function with potential parameters from [16] are slightly higher than those of [15], in the temperature range of 400-1500°K, i.e., closer to the experimental data for all mixtures (0.2, 0.4, 0.6, and 0.8 Ne), being higher by average amounts of 0.5%, 1.0%, 1.4%, and 1.8%, respectively. The best agreement (Fig. 1) appears between our experimental data and the theoretical values calculated with the modified Buckingham potential (exp-6) with potential parameters from [17]. However, in this case also, one must note that the calculated values, like those obtained with the Lennard-Jones (12-6) potential, lie systematically lower than the experimental data for all mixtures studied. The divergence between experimental and theoretical values increases with decrease in the content of the lighter component (helium) in the mixture and with increase in temperature (Table 3). For the mixtures with 0.6 and 0.8He, the divergence does not exceed the error limit of ±4%, but for the 0.4He and

TABLE 2. Potential-Function Parameters for Interaction of Similar and Dissimilar Molecules

Mixture	Potential function	Variant	ε,/k, °K	€ <u>,</u> /k, °K	e ₁₃ /k, °K	σ1, Å	σ, Å	012, Å	a1	a1	α12	Refer- ence
He — Ne	(12 - 6) (12 - 6) (exp - 6) Morse	I II I I	10,22 11,29 9,16 8,55	35,7 45,58 38,0 67,1	19,101 21,12 18,71 24,0	2,576 2,556 3,135 2,687	2,789 2,707 3,147 2,611	2,6825 2,644 3,143 2,643	 12,4 6,0		 13,46 7,0	[15] [16] [17] [18]

TABLE 3. Comparison of Smoothed and Interpolated Experimental Thermal-Conductivity Values for Neon-Helium Mixtures with Theoretical Values Calculated Using Modified Buckingham (exp-6) Potential $(\lambda \cdot 10^3, W/m \cdot {}^{\circ}K)$

	x ₁											
Т, "К	0	,2	0	,4		0,6	0,8					
<u></u>	exp.	theory	exp.	theory	exp.	theory	exp.	theory				
400	73,8	71,8 +2,8%*	91,3	89,4 +2,1%	113	113	143	143				
500	87,2	83,5 +4,4%	107	104 +2,9%	133	131 +1,5%	168	168				
600	98,9	94,5 +4,7%	122	118 +3,4%	150	149 +0,7%	192	190 +1,0%				
700	110	105 +4,8%	136	131	168	165 + 1,8%	214	211 + 1,4%				
800	121	115 +5,2%	150	143 +4,9%	185	181 +2,2%	235	231 +1,7%				
900	132	124 + 6,4%	163	155 + 5,2%	202	196 +3,1	255	250 + 2,0%				
1000	142	133 +6,8%	175	166 +5,4%	217	210 +3,3%	275	267 +3,0%				
1100	151	142 + 6,3%	187	178 +5,0%	232	224 + 3,6%	293	285 +2,8%				
1200	159	151 + 5,3%	198	188 +5,3%	247	237 +4,2%	311	301 +3,3%				
1300	168	159 + 5,7%	208	199 +4,5%	260	250 + 4,0%	328	318 + 3,1%				
1400	175	167 + 4,8%	218	209	274	263 +4,2%	345	334 +3,3%				
1500	183	175 + 4,6%	227	210 +3,7%	287	276 +4,0%	361	350 +3,1%				
	1	•			1							

*[$(\lambda_{exp} - \lambda_{theory})/\lambda_{theory}$]•100% - deviation of experimental data from theoretical data.

especially for the 0.2He mixture, the deviation exceeds the experimental uncertainty by 2.5-3%. This can be partially explained, in our opinion, for deviations up to 1-1.5% by the fact that at low helium concentrations (0.2He) impurities in the gases studied affect the results more strongly, especially helium in the neon (0.1%). We have reached this conclusion by studying the concentration dependence of the thermal conductivity in He-Ne mixtures (Fig. 2).

It should also be noted that the theoretical values obtained with the Morse potential and potential parameters from [18] lie somewhat below the calculated values obtained with the Buckingham (exp-6) potential.

By analyzing the concentration dependence of the thermal conductivity of an He-Ne mixture over the wide temperature range of 400-1500°K (Fig. 2), we have concluded that the amount of deviation of the concentration isotherms from a linear law is practically independent of temperature for an equimolar mixture.

We had arrived at analogous conclusions previously for argon helium [2] and argon neon [3] mixtures. The previous study also offers an explanation of this deviation. For an equimolar He-Ne mixture, this deviation is of the order of 17.8%. Comparison of experimental and theoretical thermal-conductivity values for binary mixtures of the light monatomic gases (He-Ne, Ne-Ar) has shown that the modified Buckingham (exp-6) potential is the one most suitable for calculation of thermal-conductivity coefficients. However, in both cases, at all concentration levels (0.2, 0.4, 0.6, and 0.8Ne), the theoretical values lie below experimental ones. In our opinion, this may be partially explained by nonconsideration of the dependence of the potential parameters themselves on temperature and by a certain imperfection in the combination rules for calculation of potential parameters for interaction of dissimilar molecules.

NOTATION

 T_{wa} , temperature of molybdenum tube wall, °K; T_{wi} , temperature of measurement wire, °K; ΔT_g , true temperature shift in gas layer, °K; \overline{T} , mean temperature, °K; Q, effective thermal flux, W; Q_c , Q_r , thermal fluxes transmitted by conduction and radiation, respectively, W; δT_{sh} , correction for temperature shift, %; λ , thermal conductivity of gas mixture, W/m° K; ε_i , σ_i , ε_{ij} , σ_{ij} , potential-function parameters for intermolecular interaction of similar and dissimilar molecules, respectively; α , slope of exponential repulsion term; x_i , concentration of lighter component (He).

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